## Applications of Group Theory

| Lectures | Tue $10: 00-11: 30$ | PHY 9.1.09 |
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|  | Thu $10: 00-11: 30$ | PHY 9.1.09 |
| Exercises | Fri $10: 00-11: 30$ | PHY 5.0.21 |

## Sheet 3

## 1. Trivial representations

Show that every symmetry operator for every group can be represented by the $(1 \times 1)$ unit matrix. Is it also true that every symmetry operator for every group can be represented by the $(2 \times 2)$ unit matrix? If so, does such a representation satisfy the Wonderful Orthogonality Theorem? Why?

## 2. Character table of the Group $D_{4}$

Using the properties of the characters introduced during the lecture, construct the character table for the group $D_{4}$. Assign to each irreducible representation the correct name according to the Mulliken notation. Finally, calculate which irreducible representations are contained in the one associated to the three dimensional vector space $\mathbb{R}^{3}$.

## Frohes Schaffen!

