## Applications of Group Theory

Sheet 3			
Exercises	Fri	10:00 - 11:30	PHY 5.0.21
Lectures	Tue Thu	10:00 - 11:30 10:00 - 11:30	PHY 9.1.09 PHY 9.1.09

## 1. Trivial representations

Show that every symmetry operator for every group can be represented by the  $(1 \times 1)$  unit matrix. Is it also true that every symmetry operator for every group can be represented by the  $(2 \times 2)$  unit matrix? If so, does such a representation satisfy the Wonderful Orthogonality Theorem? Why?

## **2.** Character table of the Group $D_4$

Using the properties of the characters introduced during the lecture, construct the character table for the group  $D_4$ . Assign to each irreducible representation the correct name according to the Mulliken notation. Finally, calculate which irreducible representations are contained in the one associated to the three dimensional vector space  $\mathbb{R}^3$ .

## **Frohes Schaffen!**