# Applications of Group Theory

PD Dr. Andrea Donarini Lectures

Exercises

H33, Mondays, 14:15 5.0.21, Wednesdays, 13:15 H34, Thursdays, 14:15

### Sheet 7

#### 1. Methane

Consider the methane molecule  $CH_4$ . We want to study the nature of the chemical bonding of the carbon with the four hydrogen atoms.

- 1. Consider the Hilbert space generated by the four 1s orbitals of the hydrogen atoms contained in a methane molecule. Construct the character system for the associated representation relative to the point group of methane. Find the irreducible representations contained in it.
- 2. Now consider the electronic structure of the carbon atom,  $1s^22s^22p^2$ , and restrict yourself to the valence orbitals. Determine the hybridization of the carbon atom compatible with the irreducible representations obtained at point 2).
- 3. Using symmetry arguments construct the molecular orbitals of methane as linear combination of carbon and hydrogen atomic orbitals. Hint: Do not try to obtain the exact orbitals. Limit yourself to the symmetry and the bonding/antibonding character of the orbitals.
- 4. Give an explicit expression for the equivalent bond orbitals of methane in terms of the valence atomic orbitals of the carbon atom.

#### 2. Molecular stability

Why would the octahedral configuration of Fig. 1b be more stable for a hypothetical  $SH_6$  than the planar configuration in Fig. 1a? Consider the angular momentum states required for the S atom to make the appropriated equivalent valence bonds to the six hydrogens in the planar  $SH_6$  hypothetical molecule.



Figure 1: Two possible configurations of the hypothetical molecule  $SH_6$ .

## Frohes Schaffen!