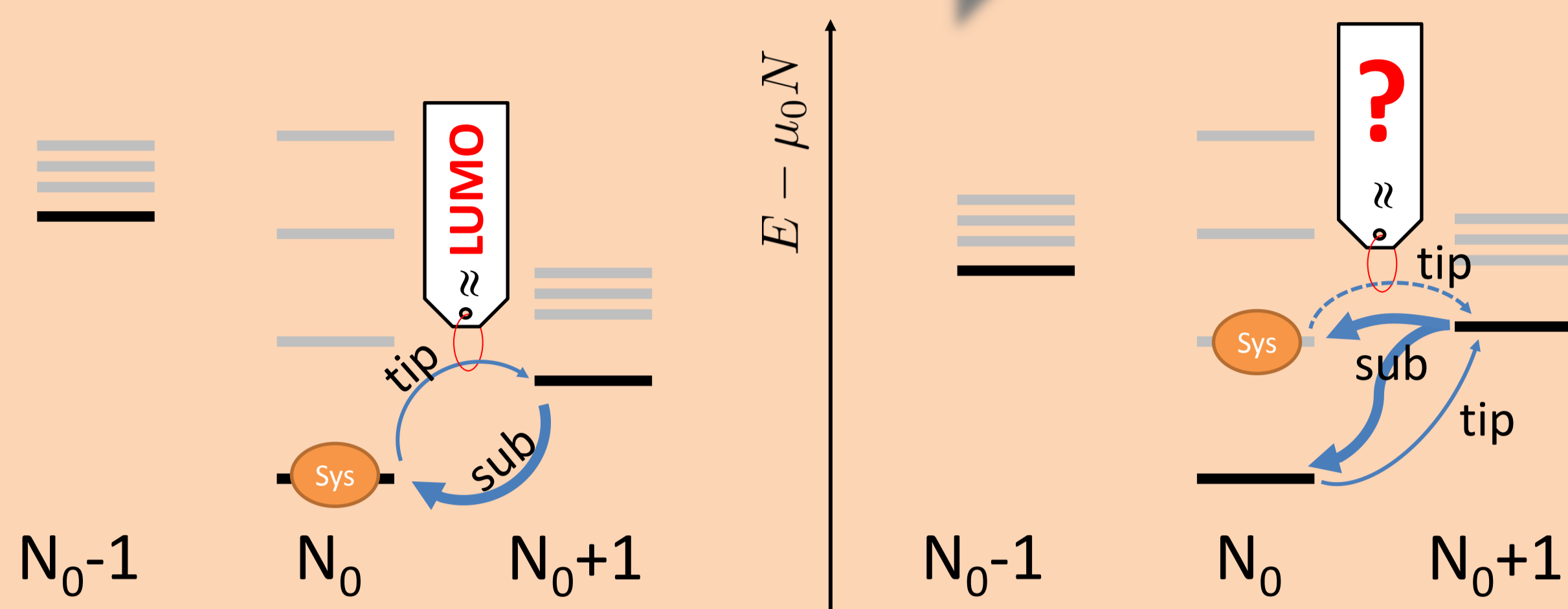


## Standard

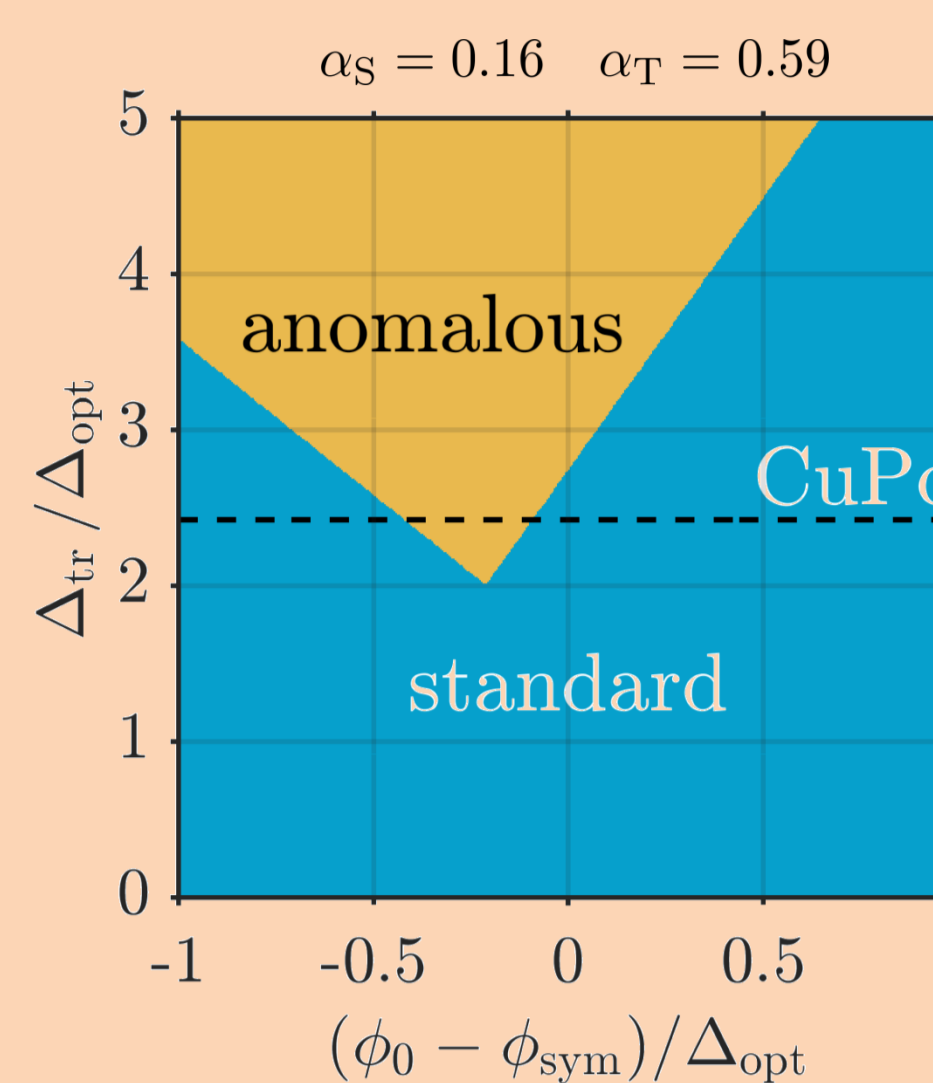
Work function modulation

## Anomalous



- Population inversion
- Topographical and spectroscopic anomalies
- Current induced control of the molecular spin

## A wide class of anomalous junctions

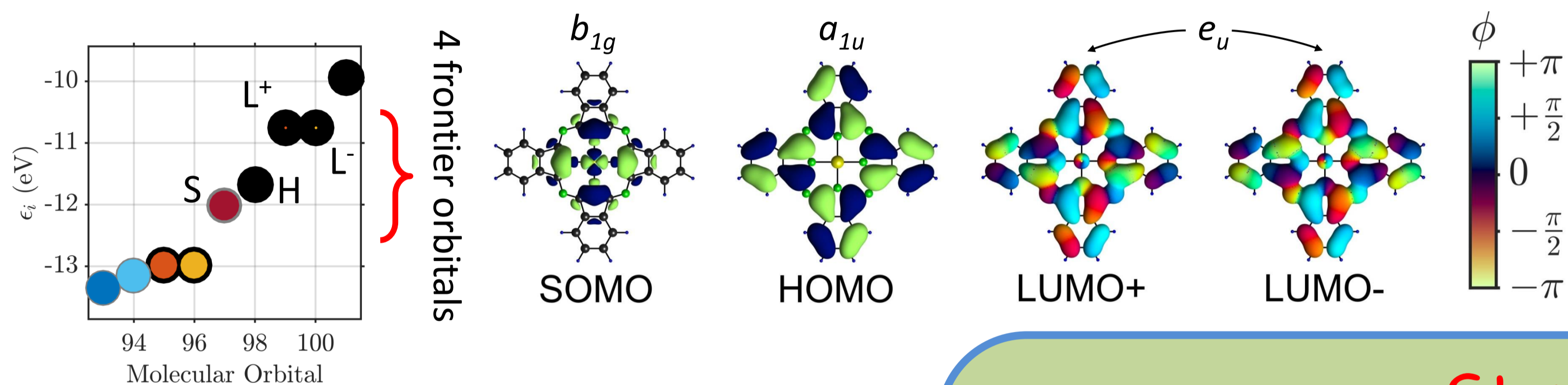


Transport gap  $\Delta_{tr} = IP - EA - 2\delta_{ic}$   
 Optical gap  $\Delta_{opt} = E_{N_0,1} - E_{N_0,0}$   
 Electroch. potentials  $\mu_{S/T} = -\phi_0 \pm \alpha_{S/T} eV_b$

- Transport gap > 2x Optical gap
- Work function close to  $\phi_{sym} = (IP + EA)/2$
- Moderate internal relaxation rate
- Strong asymmetry between substrate and tip tunnelling rates

## Many-body Hamiltonian

The single particle Hamiltonian is constructed following LCAO schemes of Harrison [1] and Slater-Koster [2].



We restrict ourselves to the Fock space spanned by:

$$|\Psi\rangle \approx |11 \dots 11 \underbrace{n_{k\uparrow} n_{k\downarrow} \dots n_{l\uparrow} n_{l\downarrow}}_{2N_d} |00 \dots 00\rangle$$

Frozen      Dynamical      Empty

The many body Hamiltonian for the molecule reads:

$$\hat{H}_{mol} = \sum_i (\epsilon_i + \Delta) \hat{n}_i + \frac{1}{2} \sum_{ijkl} \sum_{\sigma\sigma'} V_{ijkl} \hat{d}_{i\sigma}^\dagger \hat{d}_{k\sigma'}^\dagger \hat{d}_{l\sigma'} \hat{d}_{j\sigma}$$

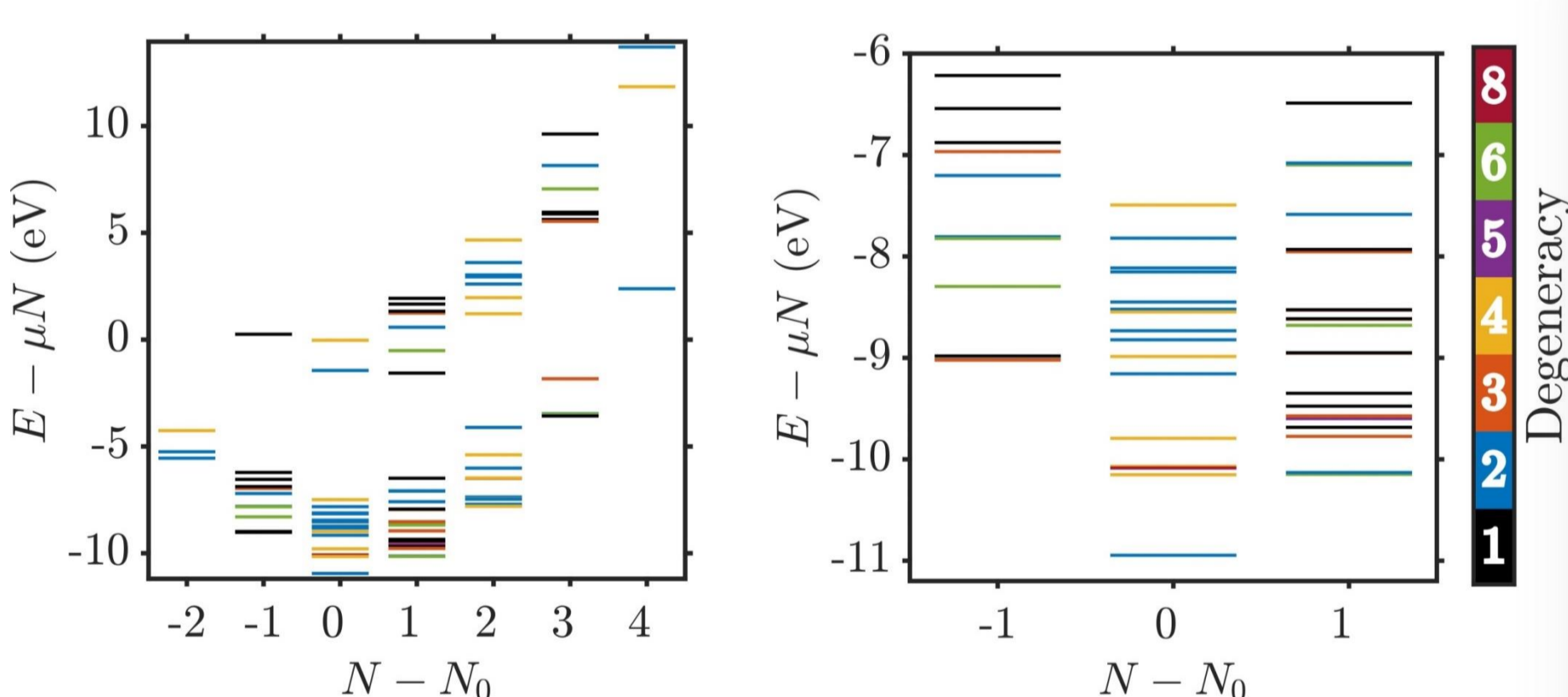
$\Delta$  is a free parameter accounting for the crystal field

$V_{ijkl}$  are ALL Coulomb integrals among dynamical orbitals

$U_S$	11.352 eV	$J_{HL}^{xx} = -J_{H+}^p$	548 meV
$U_H$	1.752 eV	$J_{+-}^{xx}$	258 meV
$U_L = U_{+-}$	1.808 eV	$J_{-}^p$	168 meV
$U_{SH}$	1.777 eV	$J_{SL}^{xx} = -J_{S+}^p$	9 meV
$U_{SL}$	1.993 eV	$J_{SH}^{xx} = J_{SH}^p$	2 meV
$U_{HL}$	1.758 eV		

The Coulomb integrals are calculated with the relative dielectric constant  $\epsilon_{mol} = 2.2$ . The atomic orbitals are of Slater type with screening charges taken from [3].

## Many-body spectrum



## Low energy many-body states

	cation			neutral			anion		
LUMO±	↑↑↑			↑↑↑			↑↑↑		
HOMO	↑↑↑			↑↑↑			↑↑↑		
SOMO	↑↑↑			↑↑↑			↑↑↑		
$E_{Nm} - E_{N0}$ (meV)	0	4	40	0	794	860	0	18	374
$S$	1	0	0	1/2	1/2	3/2	1	0	1
degeneracy	3	1	1	2	4	8	6	2	3

## Spin-crossover and transport theory

The full system is characterized by the Hamiltonian  $\hat{H} = \hat{H}_{mol} + \hat{H}_{mol-env} + \hat{H}_S + \hat{H}_T + \hat{H}_{tun}$

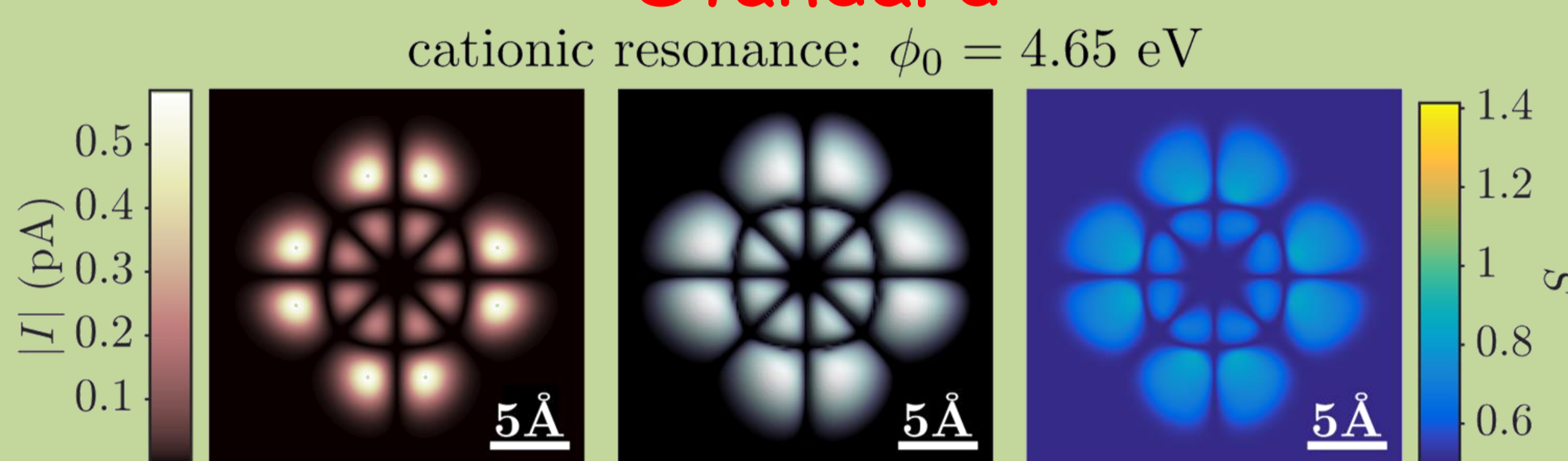
- $\hat{H}_{mol-env} = -\delta_{ic}(\hat{N} - N_0)^2$
- $\hat{H}_{S/T} = \sum_{k\sigma} \epsilon_{k\sigma}^{S/T} \hat{c}_{S/Tk\sigma}^\dagger \hat{c}_{S/Tk\sigma}$
- $\hat{H}_{tun} = \sum_{\eta k i \sigma} t_{ki}^\eta \hat{c}_{\eta k \sigma}^\dagger \hat{d}_{i\sigma} + h.c.$

The system Hamiltonian is renormalized due to image charge effects.

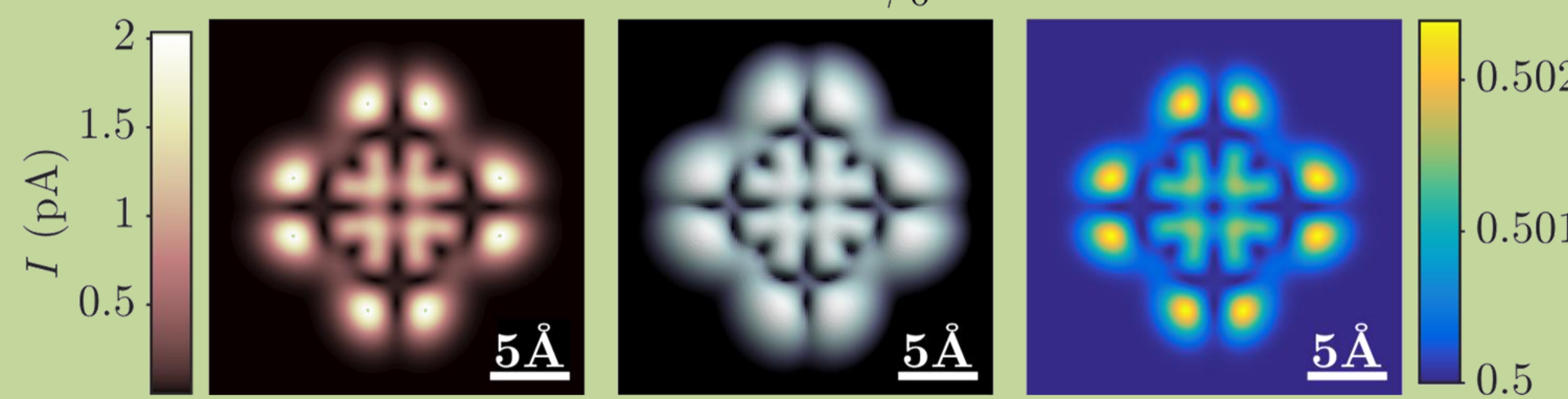
The leads are reservoirs of non interacting particles.

The tunnelling amplitudes  $t_{ki}^\eta$  encode for the geometry of the junction and are obtained analogously to [4].

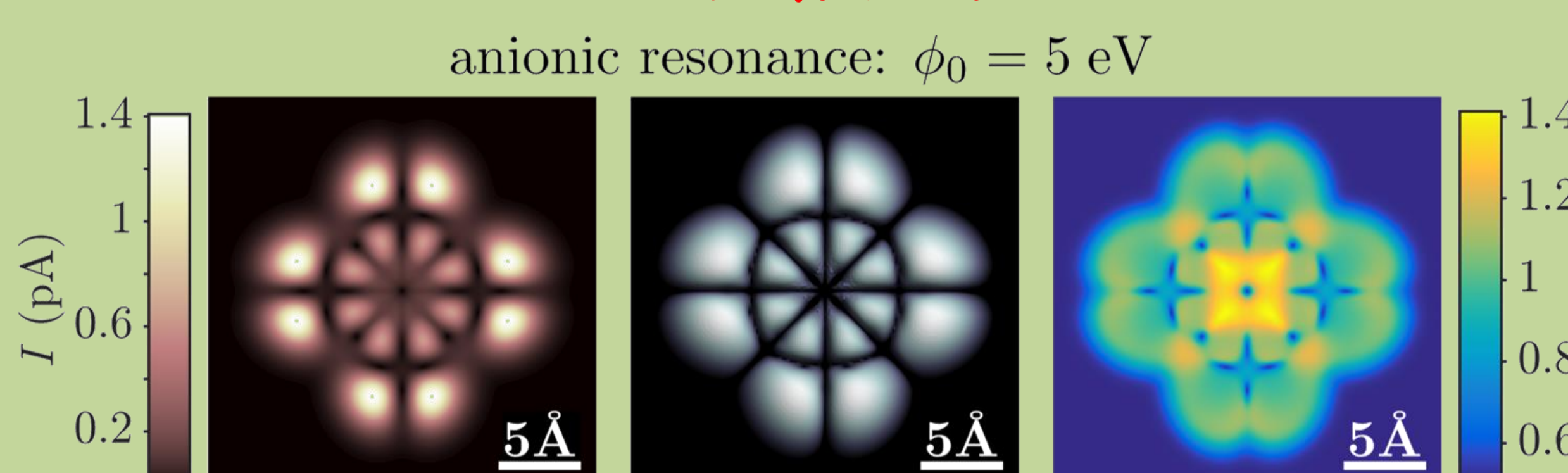
## Standard



anionic resonance:  $\phi_0 = 4.65$  eV

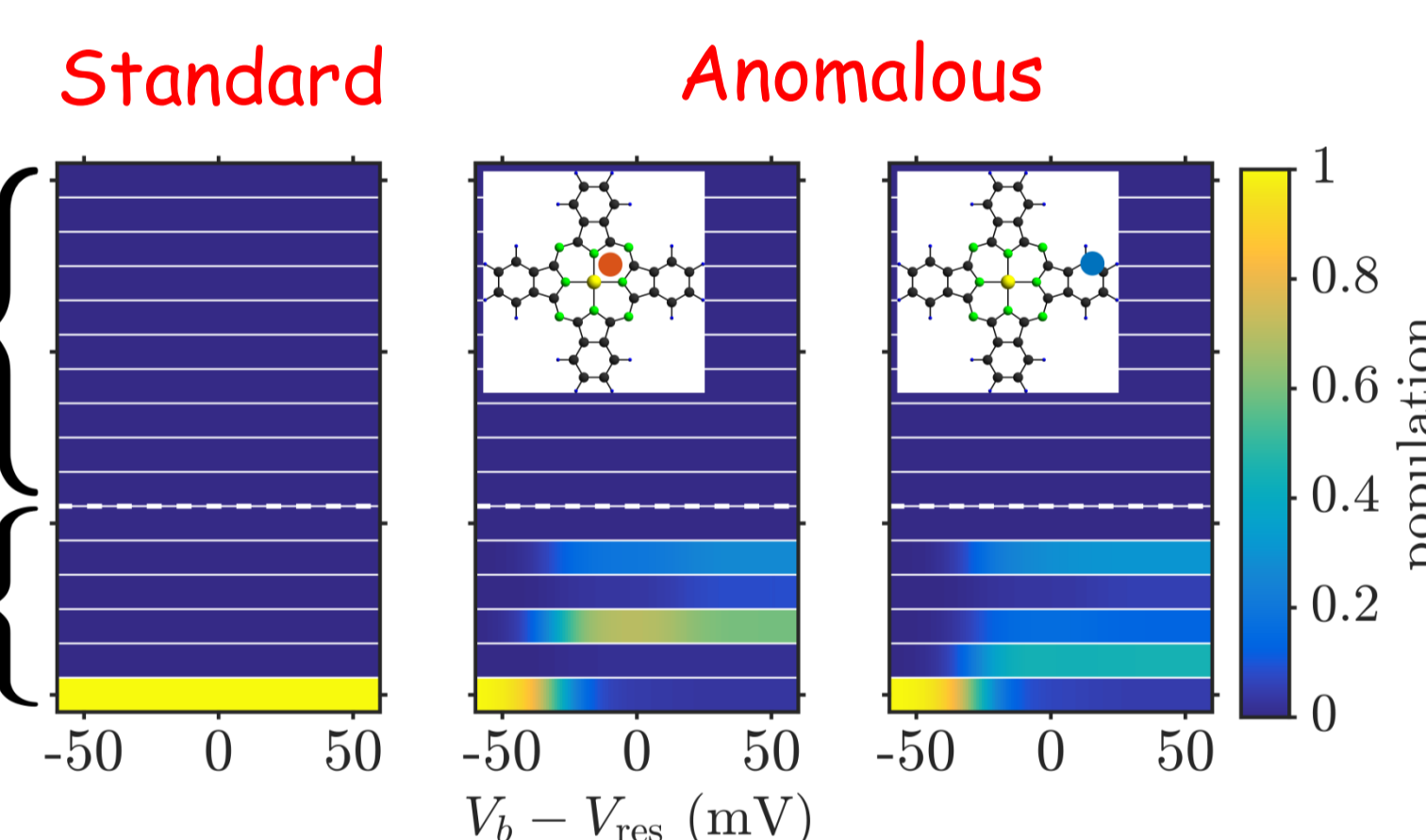
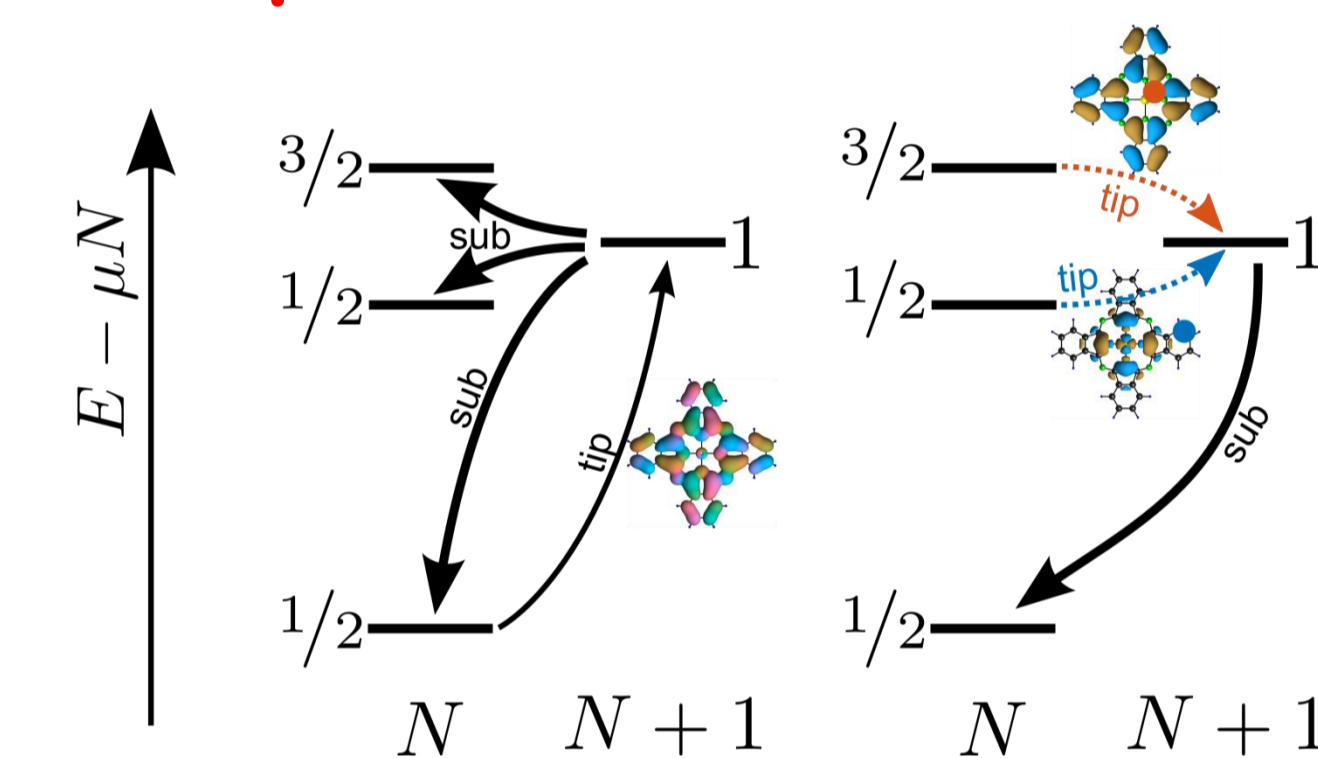


## Anomalous

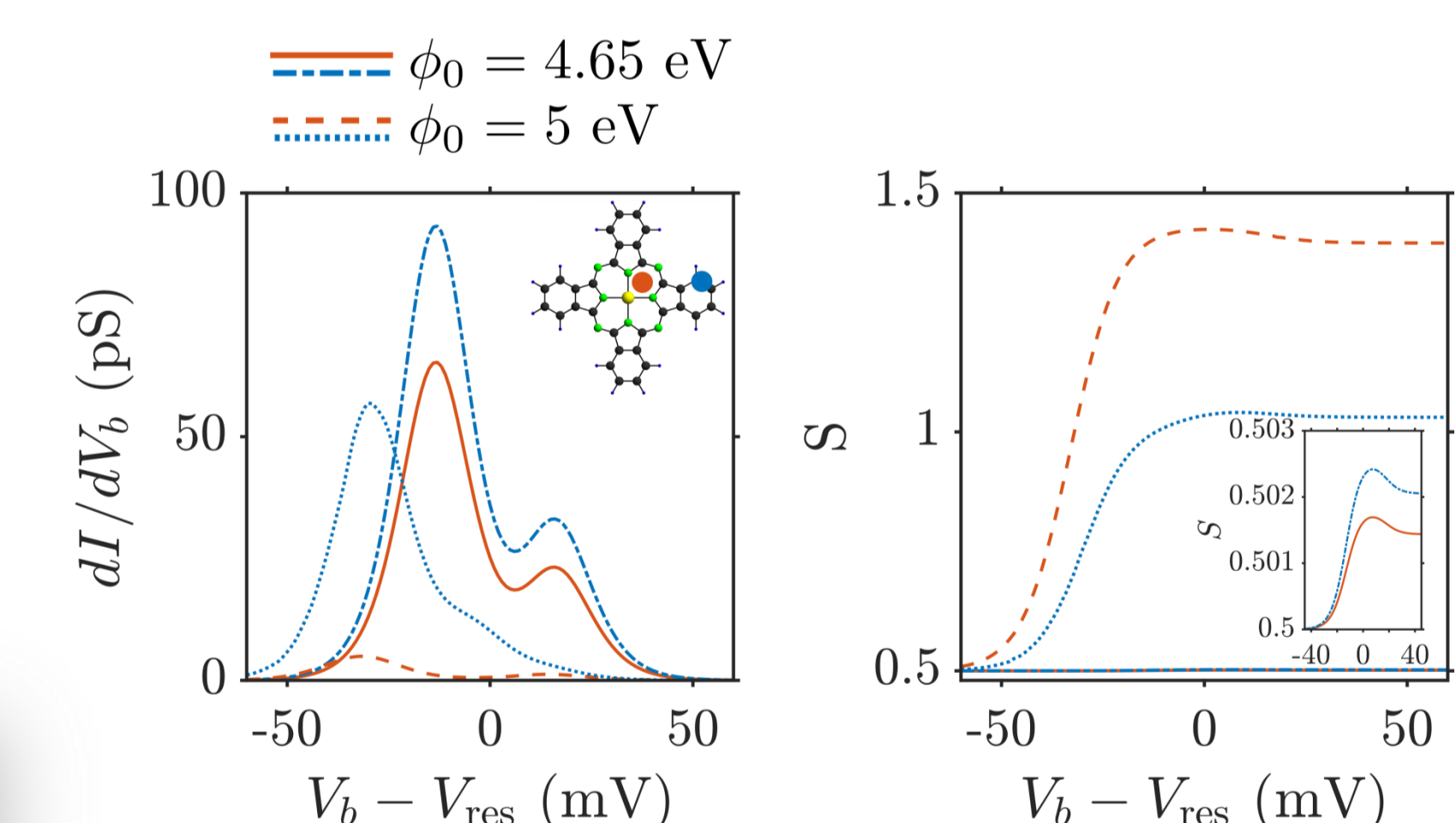


B. Siegert, A. Donarini, and M. Grifoni, arXiv:1508.04647

## Population inversion



## Spectroscopic fingerprints



The dynamics is calculated via a generalized master equation for the reduced density matrix  $\rho_{red} = \text{Tr}_{S,T}(\rho)$

$$\dot{\rho}_{red} = -\frac{i}{\hbar} [\hat{H}_{mol} + \hat{H}_{mol-env}, \rho_{red}] - \frac{i}{\hbar} [\hat{H}_{eff}, \rho_{red}] + \mathcal{L}_{tun}[\rho_{red}] + \mathcal{L}_{rel}[\rho_{red}] := \mathcal{L}[\rho_{red}]$$

Tunnelling dynamics      Phenomenological relaxation

Symmetry considerations

The molecular orbitals are eigenstates of the  $C_4$  rotation

$$R[|j\rangle] = e^{-i\phi_j} |j\rangle \Rightarrow V_{ijkl} = e^{-i(\phi_i - \phi_j + \phi_k - \phi_l)} V_{ijkl}$$

It follows that

$$V_{ijkl} \neq 0 \Leftrightarrow \phi_i - \phi_j + \phi_k - \phi_l = 0 \pmod{2\pi}$$

where one should consider

$$\phi_S = \pi, \quad \phi_H = 0, \quad \phi_{L\pm} = \pm \frac{\pi}{2}$$

Fitting parameters

	NaCl(3ML) Cu(100)	NaCl(2ML) Cu(111)
$\phi_0$ (eV)	4.65	5.00
$d$ (Å)	8.1	6.0
$\Delta$ (eV)	1.83	1.74
$\delta_{ic}$ (eV)	0.32	0.44
$\alpha_S$	0.16	0.12
$\alpha_T$	0.59	0.62
$V_{an}^{resp}$ (V)	0.81	0.95
$V_{cat}^{resp}$ (V)	0.81	1.01
$V_{cat}^{ch}$ (V)	-2.62	-2.15
$V_{cat}^{ch}$ (V)	-2.72	-2.00

$\mu_{S/T} = -\phi_0 \pm \alpha_{S/T} eV_b$

$\mathcal{L}[\rho_{red}^\infty] \equiv 0$  defines the stationary reduced density matrix.

The stationary **current** and the **molecular spin** depend on the **bias** and the **tip position**

$$I_\eta(\mathbf{r}_T, V_b) = \text{Tr}_{mol}(\hat{N} \mathcal{L}_\eta[\rho_{red}^\infty(\mathbf{r}_T, V_b)]) \quad S(\mathbf{r}_T, V_b) = \sqrt{\langle \hat{S}^2 \rangle(\mathbf{r}_T, V_b) + \frac{1}{4}} - \frac{1}{2}$$

with  $\langle \hat{S}^2 \rangle(\mathbf{r}_T, V_b) = \text{Tr}_{mol}(\hat{S}^2 \rho_{red}^\infty(\mathbf{r}_T, V_b))$

- [1] S. Froyen and W.A. Harrison, Phys. Rev. B **20**, 2420 (1979)  
 [2] J. C. Slater and G. F. Koster, Phys. Rev. **94**, 1498 (1954)  
 [3] E. Clementi and D. L. Raimondi, J. Chem Phys. **38**, 2686 (1963)  
 [4] S. Sobczyk, A. Donarini, and M. Grifoni Phys. Rev. B **85**, 205408 (2012)

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*Beilstein J. Nanotechnol.*, **6**, 2452 (2015)