## Problems to Quantum Gravity I: Canonical General Relativity WS 20/21

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Sheet 4 — Ha

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## Problem 1: Proca field

Consider the Lagrangian

$$L = \int d^3x \, \left( -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + \frac{1}{2} m^2 A_\mu A^\mu \right) \tag{1}$$

describing a massive spin 1 field  $A_{\mu}$ , where  $F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}$ . Perform the canonical analysis and show that there are 3 physical degrees of freedom per point, as opposed to 2 in the Maxwell case where m = 0.

## Problem 2: BONUS: Henneaux & Teitelboim: problem 1.26

Extend the analysis of Dirac to higher-order Lagrangians depending on the accelerations  $\ddot{q}, \ddot{q}, \ldots$  up to order k.

Hint: Treat the velocities and the accelerations as independent variables by means of Lagrange multipliers in order to get a Lagrangian that contains only first-order time derivatives. The extra added variables can be eliminated by means of their own equations and are thus auxiliary fields.